

# Heat 2D - free light version

[www.buildingphysics.com](http://www.buildingphysics.com)

Buildingphysics.com  
Software for heat transfer and ground heat

HEAT2 - Heat transfer in two dimensions

Now supporting over 40 languages!

*T(x,y)*

...

DIN (Deutsches Institut für Normung, DIN V 4108-4) is also available.

· Extensive window frame analysis has been implemented according to ISO 10077.



Support and manuals also available in German, see [www.buildingphysics.de](http://www.buildingphysics.de)



For sales and support in the CIS-countries, Latvia, Lithuania, and Estonia, see [www.buildingphysics.ru](http://www.buildingphysics.ru)

[Click here for current version update info](#)

**Free light version:** [Click here to download a free light version](#)

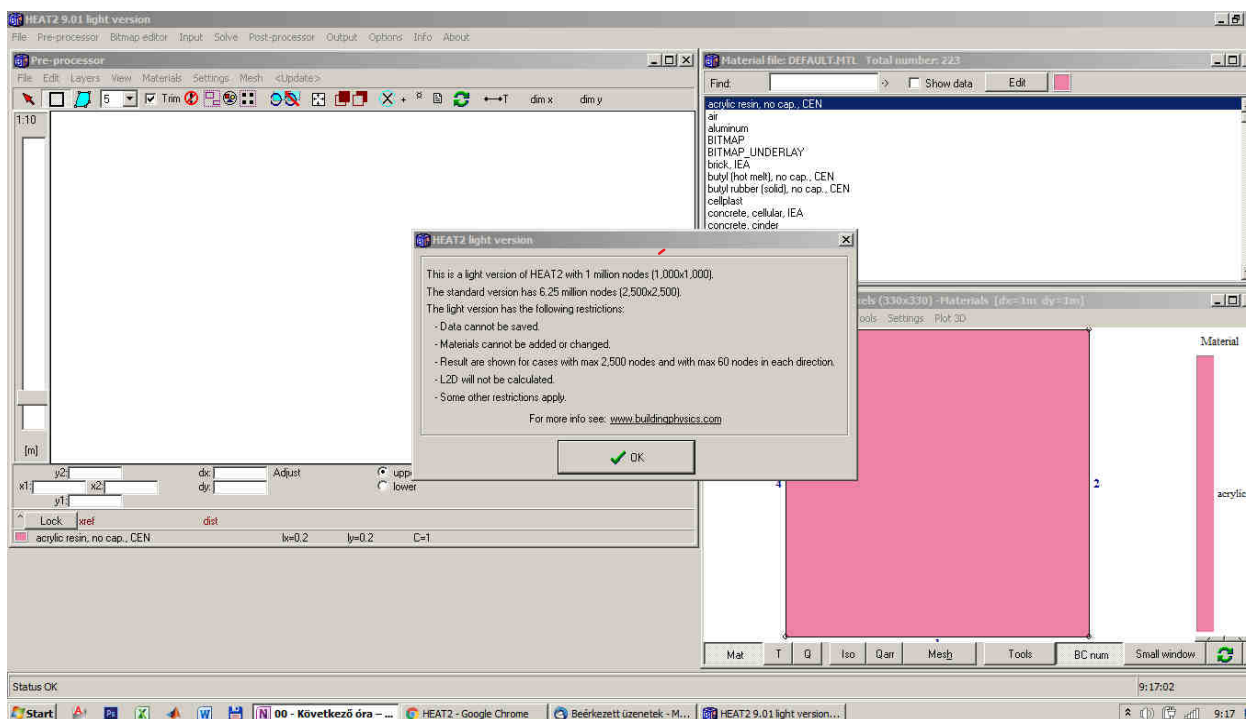


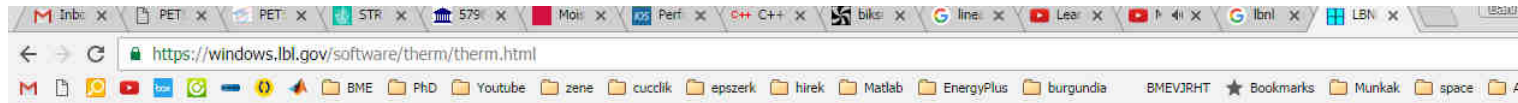
YouTube clips:

· [Input example using rectangles, polygons, and bitmaps](#)

· [Input example using bitmaps. Also shows a bitmap of a window frame that is imported and filled with different materials.](#)

**Tips for reading for beginners:** For a quick start read Chapter 4 (pages 23-27) in [Manual HEAT2 5.0](#). The example in chapter 8 (pages 117-121) would also give a short introduction. After this, look at the update manuals for [HEAT2 6.0](#), [HEAT2 7.0](#), etc. Also see the EN ISO test cases: [ISO 10211 & 10077-2](#)





## THERM

<a href="#">THERM 6.3</a> For NFRC Certification and modeling complex glazing systems	<a href="#">THERM 7.4</a> For modeling vacuum glazing, deflected glass, vertical venetian blinds, cellular shades and perforated screens
<a href="#">Forum</a> For questions about THERM	<a href="#">Forum</a> For questions about THERM
<a href="#">Knowledge Base</a> (Check here first if you are experiencing a problem with the software)	<a href="#">Knowledge Base</a> (Check here first if you are experiencing a problem with the software)
<a href="#">Documentation</a>	<a href="#">Documentation</a>
<a href="#">Tutorials</a>	<a href="#">Tutorials</a>

### Two-Dimensional Building Heat-Transfer Modeling

THERM is a state-of-the-art computer program developed at Lawrence Berkeley National Laboratory (LBNL) for use by building component manufacturers, engineers, educators, students, architects, and others interested in heat transfer. Using THERM, you can model two-dimensional heat-transfer effects in building components such as windows, walls, foundations, roofs, and doors; appliances; and other products where thermal bridges are of concern. THERM's heat-transfer analysis allows you to evaluate a product's energy efficiency and local temperature patterns, which may relate directly to problems with condensation, moisture damage, and structural integrity.

THERM's two-dimensional conduction heat-transfer analysis is based on the finite-element method, which can model the complicated geometries of building products. See [Components](#) for more details.

THERM can be used with the Berkeley Lab WINDOW program. THERM's results can be used with WINDOW's center-of-glass optical and thermal models to determine total window product U-factors and Solar Heat Gain Coefficients. These values can be used, in turn, with the [RESFEN](#) program, which calculates total annual energy requirements in typical residences throughout the United States.

[Components](#)

...

## THERM 7.4

Last Updated: 10/03/2015

If you find bugs, or have comments about this version, we now have an [online forum](#) where you can ask questions and respond to questions by others. Getting feedback from users is how we improve the program.

THERM 7 contains many new modeling features, including:

- Deflection Model
- Vacuum Glazing
- Vertical Louvered Blinds
- Perforated Screens
- Honeycomb shades
- Dynamic Glazing (Thermochromic and Electrochromic)

### Latest Version

[THERM 7.4.3](#)  
(7.4.3)  
(10/03/2015)

[Release Notes](#) -- Please read these before running this version !

This version is compatible with WINDOW 7.4.6.

- If you try to import THERM 7.4.3 files into earlier versions of WINDOW 7.3, WINDOW may crash; in this case upgrade to this latest version of WINDOW 7.4

# Windows & daylighting

## Download Registration

Before you can download software from this website you need to login. If you don't have an account, you need to Create an account first.


**This registration page will not work unless you have enabled Cookies in your browser.**

Sign in with your Account

E-mail:

Password:

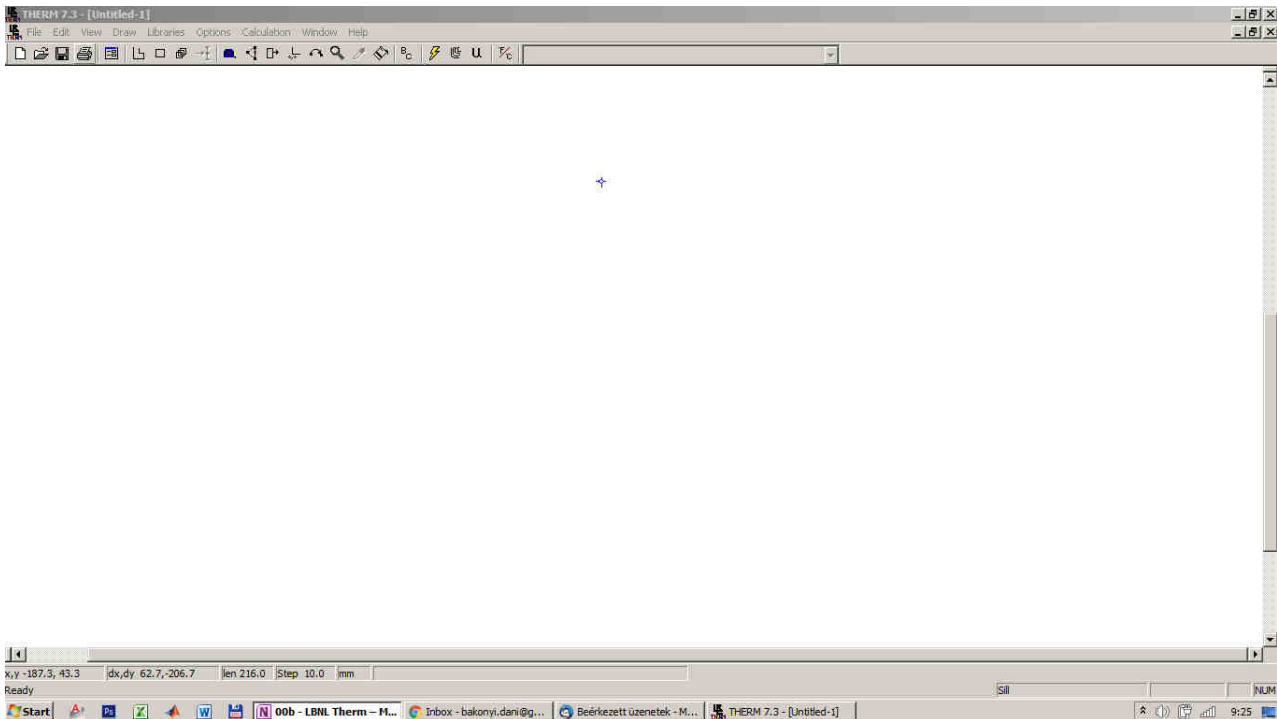
**You need to login first.  
Please enter your login details.**

Remember me on this computer. 

[Send my password...](#)

**Don't have an Account yet?**  
[Create an account now](#)

If you have questions or problems with the registration, please contact [WindowHelp@lbl.gov](mailto:WindowHelp@lbl.gov)



$$\frac{\partial}{\partial x} \lambda \frac{\partial T}{\partial x} + \frac{\partial}{\partial y} \lambda \frac{\partial T}{\partial y} + \frac{\partial}{\partial z} \lambda \frac{\partial T}{\partial z} = \cancel{\neq}$$

$$\bar{T} = x \cdot \sin \dots$$

## Lineáris algebra

vektor  $\vec{v} = \bar{v} = (v_1, v_2, v_3) = \begin{pmatrix} v_1 \\ v_2 \\ v_3 \end{pmatrix} \in \mathbb{R}^3$

mátrix  $A = \begin{pmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \\ a_{31} & a_{32} \end{pmatrix} \in \mathbb{R}^{m \times n}$

*m* (red) } index

$$A_{m \times n} = A_{3 \times 2}$$

## vektorműveletek

$$\oplus \quad \vec{u} + \vec{v} = (u_1 + v_1, u_2 + v_2, u_3 + v_3)$$

$$\ominus \quad \vec{u} - \vec{v} = (u_1 - v_1, u_2 - v_2, u_3 - v_3)$$

skalárszor.  $\alpha \cdot \vec{u} = (\alpha u_1, \alpha u_2, \alpha u_3)$

↑  
skalár

} vektor

$$\|\vec{u}\| = \sqrt{u_1^2 + u_2^2 + u_3^2} \quad (\text{norm}) \rightarrow \text{skalár}$$

$$\vec{u} \cdot \vec{v} = u_1 v_1 + u_2 v_2 + u_3 v_3 = \|\vec{u}\| \|\vec{v}\| \cos \theta \quad \uparrow$$

↑ pont szorzás v. skaláris szorzás

$$\vec{u} \times \vec{v} = \left( \underbrace{u_2 v_3 - u_3 v_2}_{\cdot i}, \underbrace{u_3 v_1 - u_1 v_3}_{\cdot j}, \underbrace{u_1 v_2 - u_2 v_1}_{\cdot k} \right) \rightarrow \text{vektor}$$

$$\|\vec{u} \times \vec{v}\| = \|\vec{u}\| \|\vec{v}\| \sin \theta$$

↑

$$\|\vec{v} \times \vec{u}\|$$

matrix műveletek

elemek  $a_{ij}$   $b_{ij}$

⊕  $C = A + B \sim c_{ij} = a_{ij} + b_{ij}$

$$\begin{pmatrix} 1 & 2 & | & 4 & 6 & | & 5 & 8 \\ 3 & 4 & | & 7 & 9 & | & 10 & 13 \end{pmatrix} =$$

⊖  $c_{ij} = a_{ij} - b_{ij}$

matrix szorzás

$A \in \mathbb{R}^{m \times n}$

$B \in \mathbb{R}^{n \times \ell}$

$\rightarrow C = A \cdot B \in \mathbb{R}^{m \times \ell}$

↑ sor  
↑ oszlop

$$c_{ij} = \sum_{k=1}^n a_{ik} b_{kj}$$

$$m \left\{ \begin{array}{cc|cc} \textcircled{1} & \textcircled{2} & 7 & 10 \\ \textcircled{3} & \textcircled{4} & 15 & 22 \end{array} \right\} \begin{array}{l} \text{v}_1 \\ \text{v}_2 \end{array}$$

$$A_{2 \times 2} \quad \begin{array}{c} m \\ n \end{array} \quad \begin{array}{c} u \\ l \end{array} \quad \begin{array}{c} 1 \\ 2 \end{array} \quad \begin{array}{c} v_{2 \times 2} \\ l \end{array}$$

$$\begin{array}{c} 1 \quad 2 \\ 3 \quad 4 \end{array} \quad \left| \begin{array}{c} 1 \\ 2 \end{array} \right|$$

$$A \cdot v_{\underline{2}} = u$$

$$\begin{array}{c} a_{11} \quad a_{12} \\ a_{21} \quad a_{22} \\ a_{31} \quad a_{32} \end{array} \begin{array}{c} x_1 \\ x_2 \end{array} = \begin{array}{c} a_{11}x_1 + a_{12}x_2 \\ a_{21}x_1 + a_{22}x_2 \\ a_{31}x_1 + a_{32}x_2 \end{array} = x_1 \begin{array}{c} a_{11} \\ a_{21} \\ a_{31} \end{array} + x_2 \begin{array}{c} a_{12} \\ a_{22} \\ a_{32} \end{array}$$

$$A_{3 \times 2} \cdot X_{2 \times 1} = Y_{3 \times 1}$$

$$\vec{y} = T_1(\vec{x}) = A \cdot \vec{x}$$

$$f: \mathbb{R} \rightarrow \mathbb{R} \quad \Leftrightarrow T_r \quad \mathbb{R}^n \rightarrow \mathbb{R}^n$$

$$f(x) \quad \Leftrightarrow T_r(\vec{x}) = A \cdot \vec{x}$$

$$g \circ f = g(f(x)) \quad \Leftrightarrow T_r(T_1(\vec{x})) = B \cdot A \cdot \vec{x}$$

$$g \circ f = g(f(x)) \Leftrightarrow T_B(T_A(\vec{x})) = B \cdot A \cdot \vec{x}$$

$$f^{-1} \Leftrightarrow A^{-1}$$

$$\ln(x) \quad e^x$$

~~$$\ln(x) e$$~~

$$\ln(e^x) = x$$

$$A^{-1} A = \mathbb{I} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix} = \begin{pmatrix} 1+0 \\ 2+0 \\ 3+0 \end{pmatrix} = \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix}$$



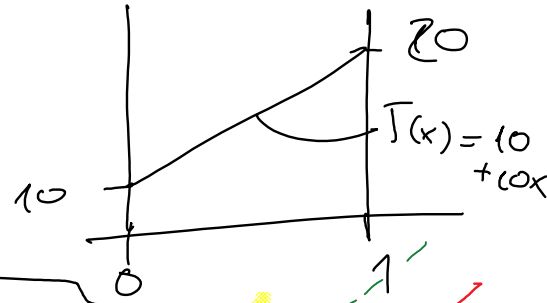
02 - véges differencia

2016. szeptember 23.  
12:59

$$\frac{\partial}{\partial x} \lambda_x \frac{\partial T}{\partial x} + \frac{\partial}{\partial y} \lambda_y \frac{\partial T}{\partial y} + \frac{\partial}{\partial z} \lambda_z \frac{\partial T}{\partial z} = 0$$

$$\frac{\partial^2 T}{\partial x^2} = 0$$

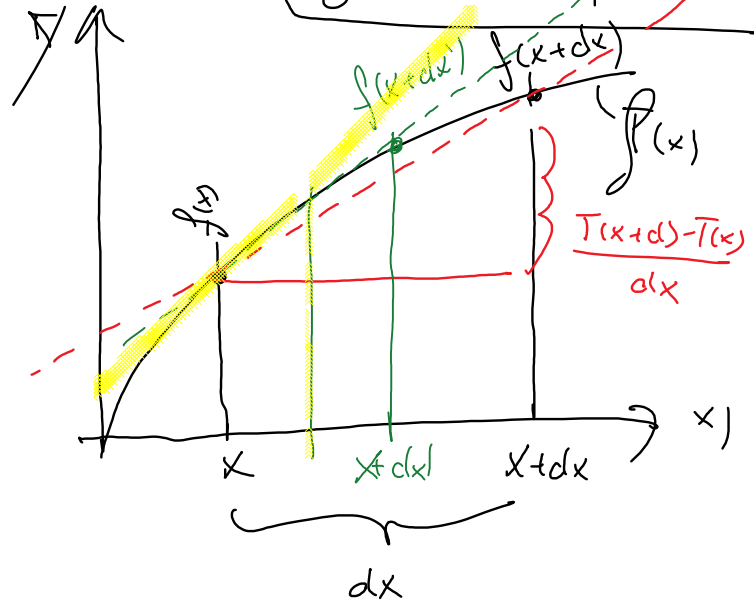
• 1D  
•  $\lambda = 1$



$$\lim_{dx \rightarrow 0} \frac{T(x+dx) - T(x)}{dx} = T'(x)$$

differencia-  
hányados

differenciál-  
hányados



$$\frac{\partial T}{\partial x} \approx \frac{T(x+dx) - T(x)}{dx}$$

haladó - differencia  
(forward difference)

$$\frac{\partial T}{\partial x} \approx \frac{T(x) - T(x-dx)}{dx}$$

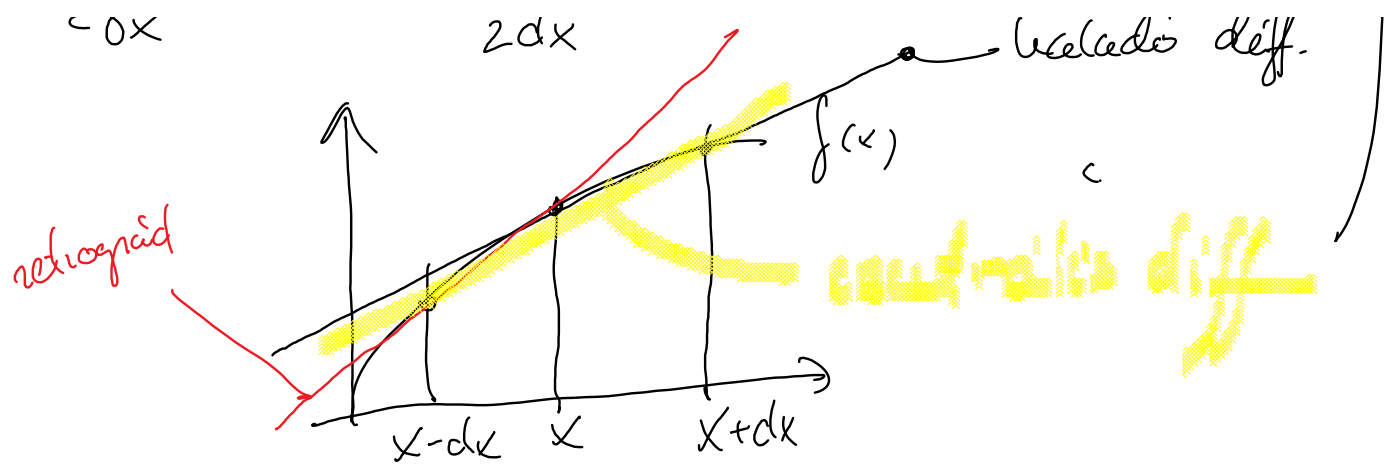
retrográd - differencia  
(backward - difference)

$$\frac{\partial T}{\partial x} \approx \frac{T(x+dx) - T(x-dx)}{2dx}$$

centrális differencia

haladó diff.

véges differencia

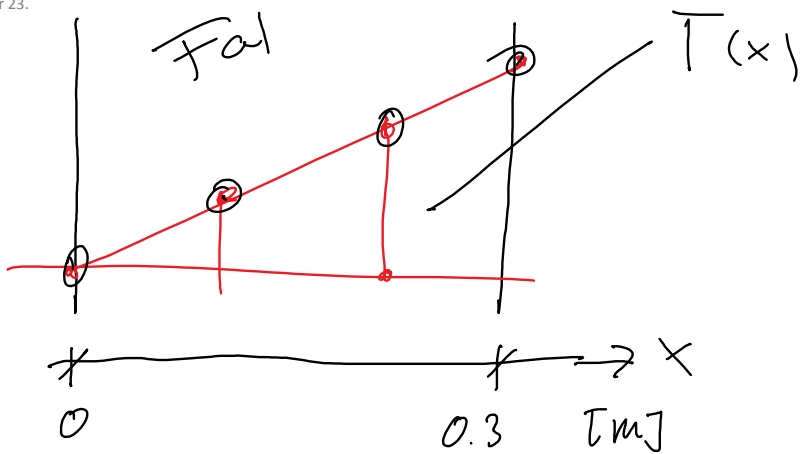


2. rendű véges differenciák

$$\begin{aligned}
 \frac{\partial^2 T}{\partial x^2} &\approx \frac{T'(x) - T'(x-dx)}{dx} = \frac{\frac{T(x+dx) - T(x)}{dx} - \frac{T(x) - T(x-dx)}{dx}}{dx} = \\
 &= \frac{T(x+dx) - 2T(x) + T(x-dx)}{dx^2}
 \end{aligned}$$

03 - egy konkrét példa

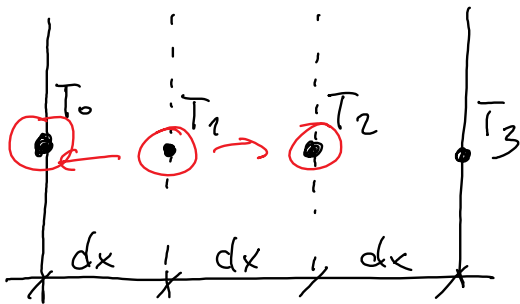
2016. szeptember 23.  
13:13



BC:  
 $T(x=0) = 10 [C]$   
 $T(x=0.3) = 20 [C]$

$$\lambda \frac{\partial^2 T}{\partial x^2} = \phi$$

1.



$dx = 0.1 [m]$

diszkrétizáció

2.

diszkrétizált egyenletek felírása

$$T_1 = \frac{\lambda T_{(x-dx)} - 2\lambda T_{(x)} + \lambda T_{(x+dx)}}{\lambda T_0 - 2\lambda T_1 + \lambda T_2} = 0$$

$$\frac{\lambda T_{(x-dx)} - 2\lambda T_{(x)} + \lambda T_{(x+dx)}}{dx^2} = 0$$

$$\lambda \frac{\partial^2 T}{\partial x^2} = 0$$

$x=1$

$T_1:$   $\frac{\lambda}{dx^2} T_0 - \frac{2\lambda}{dx^2} T_1 + \frac{\lambda}{dx^2} T_2 = 0$

$T_2:$   $\frac{\lambda}{dx^2} T_1 - \frac{2\lambda}{dx^2} T_2 + \frac{\lambda}{dx^2} T_3 = 0$

$T_0 = 10$

$T(x)$   
 lineáris  
 egyenlet rendszer

$\lambda = 1$   
 $\lambda = 0.01$

$$l_0 = 10$$

$$T_3 = 20$$

$$\lambda = 0.01$$
$$dx = 0.1$$

(3) peremfeltételek bevezetése

$$-\frac{2\lambda}{dx^2} T_1 + \frac{\lambda}{dx^2} T_2 = -\frac{\lambda}{dx^2} 10$$

$$\frac{\lambda}{dx^2} T_1 - \frac{2\lambda}{dx^2} T_2 = -\frac{\lambda}{dx^2} 20$$

$$\begin{pmatrix} -\frac{2\lambda}{dx^2} & \frac{\lambda}{dx^2} \\ \frac{\lambda}{dx^2} & -\frac{2\lambda}{dx^2} \end{pmatrix} \begin{pmatrix} T_1 \\ T_2 \end{pmatrix} = \begin{pmatrix} -\frac{\lambda}{dx^2} 10 \\ -\frac{\lambda}{dx^2} 20 \end{pmatrix}$$

U.C

A  
↑  
mátrix

$\vec{x} = \vec{b}$   
↑  
ismeretlenek vektora

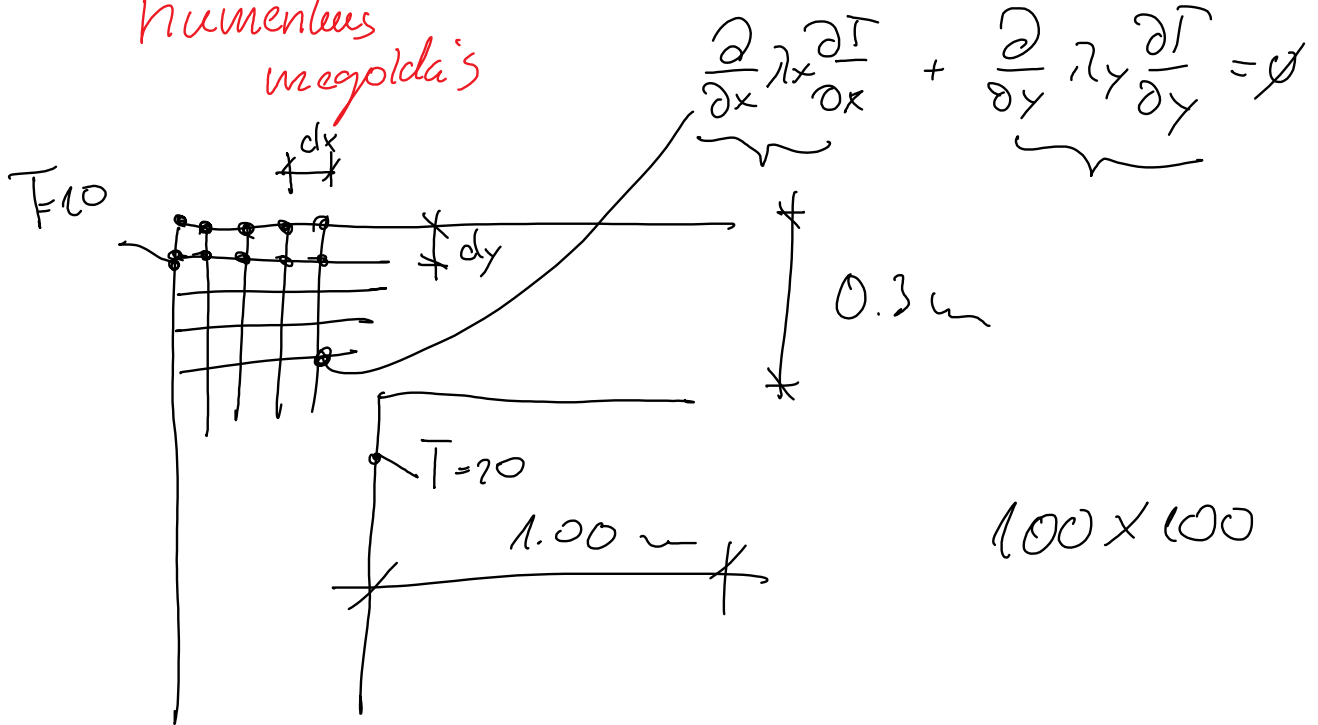
← konstansok vektora

$$\vec{x} = \begin{pmatrix} T_1 \\ T_2 \end{pmatrix} = \begin{pmatrix} 3.33 \\ 6.66 \end{pmatrix}$$

$$\Leftrightarrow T(x) = 10x + 20$$

analitikus megoldás

numerikus  
megoldás



$$\begin{array}{c}
 \text{A} \\
 \begin{pmatrix}
 1 & 0 & 0 & 0 \\
 \frac{\partial}{\partial x^2} & -\frac{2\lambda}{\partial x^2} & \frac{\lambda}{\partial x^2} & 0 \\
 0 & \frac{\partial}{\partial x^2} & -\frac{2\lambda}{\partial x^2} & \frac{\partial}{\partial x^2} \\
 0 & 0 & 0 & 1
 \end{pmatrix}
 \end{array}
 \begin{array}{c}
 \bar{x} \\
 \begin{pmatrix}
 T_0 \\
 T_1 \\
 T_2 \\
 T_3
 \end{pmatrix}
 \end{array}
 =
 \begin{array}{c}
 \underline{b} \\
 \begin{pmatrix}
 10 \\
 \frac{\partial}{\partial x^2} \\
 0 \\
 20
 \end{pmatrix}
 \end{array}$$

04 - az egyenletrendszer megoldása

2016. szeptember 23.  
13:36

$$A \bar{x} = b$$

① mátrix inverz

$$\underbrace{A^{-1} A} \cdot \bar{x} = A^{-1} \cdot b$$

$$I \cdot \bar{x} = A^{-1} \cdot b$$

$$\bar{x} = A^{-1} \cdot b$$

gépide !!!

② Gauss-Jordan elimináció  
direkt módszer

műveletek  $\nearrow$  egyik sor n-storését + / - másik sorhoz  
 $\rightarrow$  kicserélhetek két sort  
 $\searrow$  sor skálár szorzása  
 $A \cdot \bar{x} = b$

$$\begin{matrix} \textcircled{1} & 2 & \left| \begin{matrix} x_1 \\ x_2 \end{matrix} \right| = \begin{matrix} 5 \\ 21 \end{matrix} \\ \textcircled{3} & 9 & \end{matrix}$$

cél:  $\begin{matrix} 1 & 2 & \dots & \dots \\ 0 & 1 & \dots & \dots \\ 0 & 0 & 1 & \dots \end{matrix} \left| \begin{matrix} x_1 \\ x_2 \\ x_3 \\ \vdots \end{matrix} \right| = \begin{matrix} b_1 \\ b_2 \\ b_3 \\ \vdots \end{matrix}$

$$\boxed{3} \quad 9 \quad | \quad x_2 \quad | \quad (21)$$

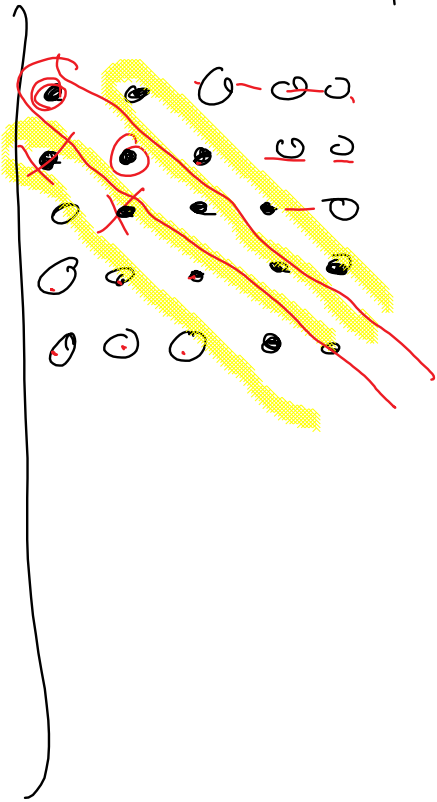
$$\begin{pmatrix} \dots & \dots & \dots & \dots \\ 0 & 0 & 1 & \dots \\ \dots & \dots & \dots & \dots \\ 0 & 0 & 0 & \dots \end{pmatrix} \begin{matrix} x_3 \\ \vdots \\ x_2 \end{matrix} = \begin{matrix} b'_2 \\ b'_3 \\ \vdots \\ b'_n \end{matrix}$$

2.sor - 3x l.sor

$$\left[ \begin{array}{cc|c} 1 & 2 & x_1 \\ 0 & \textcircled{3} & x_2 \end{array} \right] = \left[ \begin{array}{c} 5 \\ 6 \end{array} \right]$$

2.sor / 3

$$\left[ \begin{array}{cc|c} 1 & 2 & x_1 \\ 0 & 1 & x_2 \end{array} \right] = \left[ \begin{array}{c} 5 \\ 2 \end{array} \right] \rightarrow x_2 = 2$$



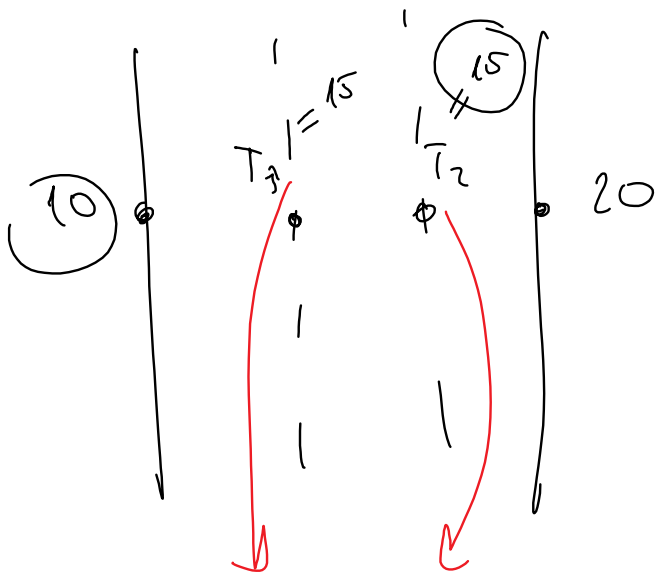
$$\begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \\ \vdots \\ x_n \end{pmatrix} = \begin{pmatrix} b_1 \\ b_2 \\ b_3 \\ b_4 \\ \vdots \\ b_n \end{pmatrix}$$

$\textcircled{3}$  iterativ solver

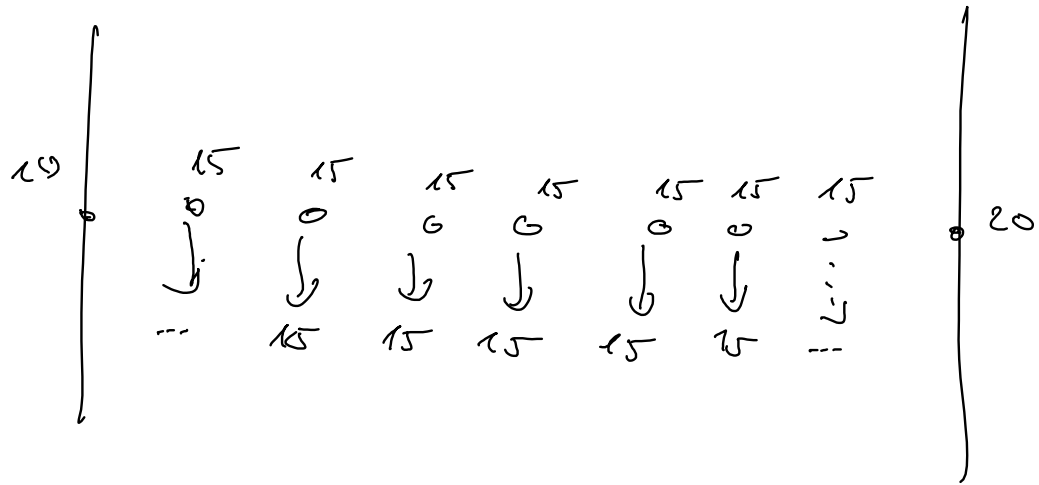
$$X_{EM} = \begin{vmatrix} 10 \\ 10 \end{vmatrix}$$

$$\begin{vmatrix} 1 & 2 \\ 3 & 9 \end{vmatrix} \begin{vmatrix} x_1 \\ x_2 \end{vmatrix} = \begin{vmatrix} 5 \\ 21 \end{vmatrix} \rightarrow \begin{vmatrix} x_1 \\ x_2 \end{vmatrix} = \begin{vmatrix} 1 \\ 1 \end{vmatrix}$$

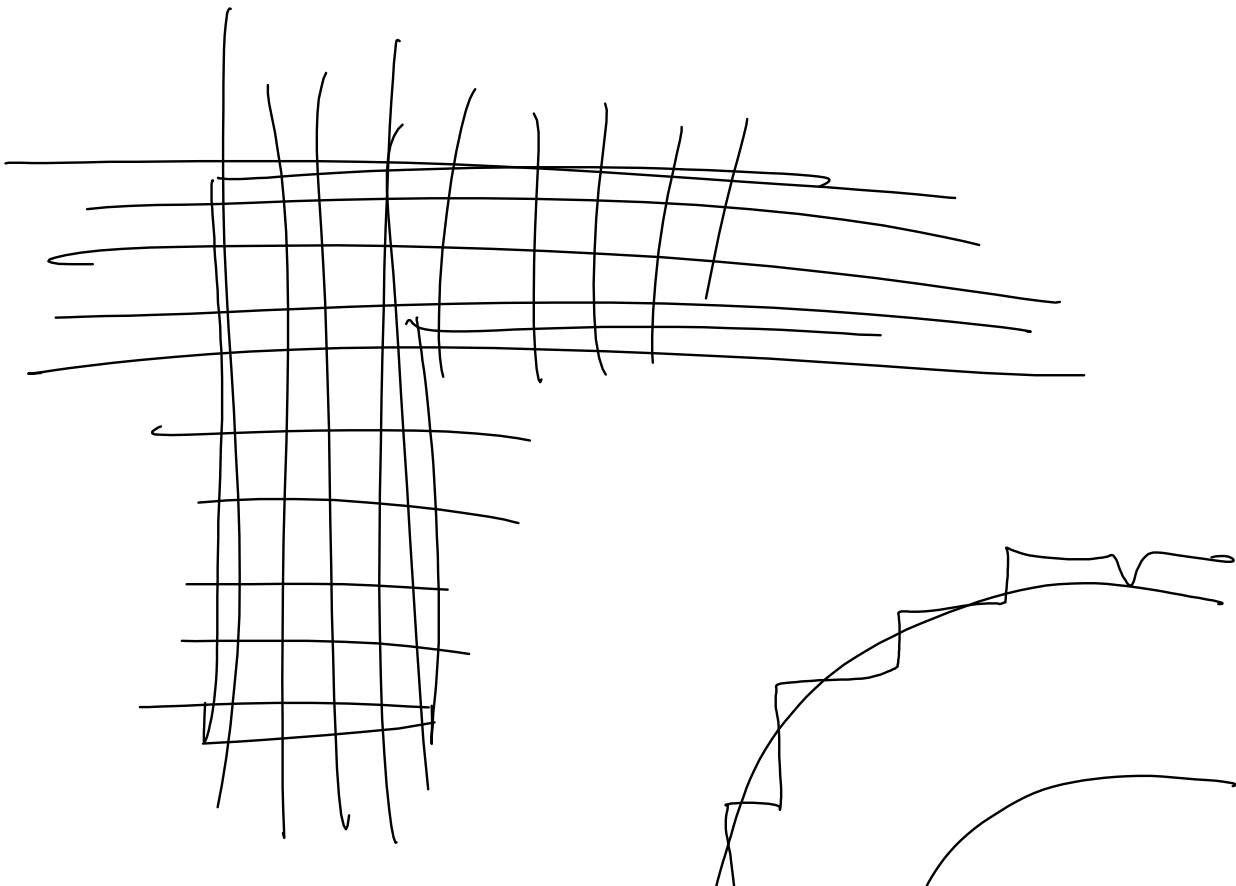
The diagram shows a system of linear equations represented as a matrix multiplication. On the left, a coefficient matrix  $\begin{vmatrix} 1 & 2 \\ 3 & 9 \end{vmatrix}$  is multiplied by a variable vector  $\begin{vmatrix} x_1 \\ x_2 \end{vmatrix}$ . The variable  $x_1$  is circled in red, and  $x_2$  is circled in green. To the right of the first matrix, there is an equals sign followed by a constant vector  $\begin{vmatrix} 5 \\ 21 \end{vmatrix}$ . A red arrow points from the top row of the first matrix to the top row of the second matrix, and a green arrow points from the bottom row of the first matrix to the bottom row of the second matrix. Further to the right, another equals sign is followed by a simplified variable vector  $\begin{vmatrix} x_1 \\ x_2 \end{vmatrix}$ . Above the first matrix, the number 10 is written in green with a double line pointing to the  $x_1$  variable. Below the first matrix, the number 10 is written in red with a double line pointing to the  $x_2$  variable.







$$\Delta T_{max} = 0.0001 \text{ [K]}$$



' | v |

